BASE CASE SIMULATION OF A SEMI-BATCH EMULSION COPOLYMERIZATION PROCESS: APPLICATION TO STYRENE/BUTADIENE SYSTEM

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Abstract

It has been long recognized that emulsion polymerization is a complex heterogeneous process involving transport of monomers, free radicals, and other species between aqueous phase and organic phase. Though there are a number of models available in the literature, most of them deal only with specific aspects in emulsion polymerization and are far from being general. To simulate this complicated process and to achieve an adequate level of understanding, a Polymers Plus software from Aspen Technology, Inc. was used. The objective of this work is to illustrate the principle of use of Polymers Plus, simulate, and analyze the free-radical seeded emulsion copolymerization of styrene-butadiene process model in a semi-batch reactor. The base case simulation can be used to gain process understanding by analyzing how process variables and operating conditions during the course of a semi-batch reactor affect the product quality.

Keywords: Polymers Plus, Emulsion Copolymerization, Simulation, Semi Batch Reactor, Styrene/butadiene

Abstrak

Telah diketahui sejak lama bahwa polimerisasi emulsi merupakan sebuah proses heterogen yang kompleks, yang meliputi perpindahan monomer, radikal bebas, dan senyawa lainnya dalam fasa air dan fasa organik. Walaupun dalam literatur terdapat berbagai model, sebagian besar hanya membahas tentang aspek-aspek khusus dalam polimerisasi emulsi yang belum berlaku umum. Untuk melakukan simulasi serta meningkatkan pemahaman tentang proses yang kompleks ini, digunakan perangkat lunak Polymers Plus dari Aspen Technology, Inc. Penelitian ini bertujuan untuk memberikan ilustrasi tentang prinsip penggunaan Polymers Plus serta melakukan simulasi dan analisis tentang model untuk proses kopolimerisasi emulsi styrene-butadiene dengan free radical seeded dalam reaktor semi batch. Simulasi ini dapat digunakan untuk memperoleh pemahaman proses dengan menganalisis pengaruh variabel-variabel proses dan kondisi operasi dalam reaktor semi batch terhadap kualitas produk.

Kata Kunci: Polymers Plus, Kopolimerisasi Emulsi, Simulasi, Reaktor Semi Batch, Stiren/butadien

1. Introduction

Emulsion polymers, or latexes, are polymer particles with sub-micron size dispersed in water. Stabilization of the particles is achieved by surfactants that tend to concentrate at the polymer surface. In the 1930's, the first emulsion polymerized styrene-butadiene rubber (SBR) known as Buna S was prepared by I. G. Farbenindustrie in Germany. Emulsion polymerized styrene-butadiene rubber (SBR) is one of the most widely used polymer in the world today. It is an industrially important process for the production of polymers used as synthetic rubber materials, inks, coating applications such as paints and adhesives; nonwoven fabrics. SBR production technology is detailed by Blackley and Lovell (Blackley, 1997; Lovell, 1997). About 2.5 million tons (International Institute of Synthetic Rubber Producers (IISRP), 2004) of SBR are annually produced.

The polymerization is usually carried out using water as the dispersion medium. This makes emulsion polymerization less detrimental to the environment than other processes in which volatile organic liquids are used as a medium. In addition, emulsion polymerization offers distinct processing advantages for the production of polymers. Unlike in bulk or solution polymerization, the viscosity of the reaction mixture does not increase as dramatically as polymerization progresses. For this reason, the emulsion polymerization offers excellent heat transfer throughout the course of polymer particles. This process is always chosen when the polymer product is used in latex form. In emulsion polymerization, free-radical propagation reactions take place in particles isolated from each other by the intervening dispersion medium. This reduces termination rates, giving high polymerization rates, and simultaneously makes it possible to produce high molecular weight polymers (Lovell, El-Aaser, 1997).

Many polymerization processes are neither batch nor continuous, but rather intermediate between two. These processes may be termed semibatch or semicontinuous. A reaction may be done in a semibatch or semicontinuous mode, or in stages for countless reasons. Common examples include promoting more desirable reaction path; to achieve a desired morphology; to adjust or maintain stoichiometry; to obtain a desired chain length, composition, or sequence length distribution; to modify the polymer product in some way; and for control purpose.

Batch and semi-batch processes are usually dedicated to the low volume production of high value products or specialty grades. In semi-batch processes (also referred to as semi-continuous batch processes), only part of the total reaction formulation is introduced at the beginning of the reaction, the remainder is being added, according to a predetermined schedule, during the course of the emulsion polymerization. In a typical semi-batch process employing in-situ seeding, the heated initial charge of different materials is used for the production of seed particles; the radicals generated from the initiator become surface active and enter micelles to form particles (Blackley, 1997).

The strategy of seeded emulsion polymerization is widely utilized, not only in batch processes, but also in semi-batch and continuous processes. In seeded polymerization, particle nucleation is separated from particle growth. Seeded emulsion polymerization has two major advantages. Firstly, further complication of nucleation kinetics is avoided due to the absence of particle nucleation. Secondly, physical properties (such as particle size distribution and particle concentration) of the preformed particles can be fixed in advance in which the particle size distribution will be narrow if the seed stage is short (Blackley, 1997).

Once the particles specifications or the reaction temperature are met, monomers, and other ingredients, such as emulsifier, water, and initiators are continuously added to the reactor according to some feed procedures until the end of the batch. The surfactant amount must be selected so that it is just sufficient to maintain the colloidal stability of the preformed latex particles, but not so high as to generate new particles. It should be almost instantaneously mixed up with reactor contents. The particles are grown to the desired physical properties. For all semi-batch processes, the rate at which monomer is introduced to the reaction is of crucial importance because it controls the availability of monomer for polymerization and hence the concentration of monomer in the particles. The popularity of this method is easily understood; it grants safe operation and good control of both reaction exothermic and characteristics of the product. This kind of semi-batch operation is also favored because it provides great flexibility (Lovell, El-Aaser, 1997).

The objective of this work is to illustrate the principle of use of Polymers Plus and to simulate and analyze the free-radical seeded emulsion

copolymerization of styrene-butadiene process model in a semi-batch reactor. The base case simulation can be used to gain process understanding by analyzing how process variables and operating conditions during the course of a semi-batch reactor affect the product quality.

Integrated with Aspen Plus, Polymers Plus is a general-purpose modeling system for simulating polymer and oligomer manufacturing operations. Polymers Plus contains various advanced polymer science and engineering technologies for polymer process modeling. These include: component characterization; physical properties and phase equilibria; databanks; polymerization kinetics and reaction mechanisms; and polymer product properties.

2. Fundamental

The rough understanding of how emulsion polymerization proceed had to wait until the late 1940s, for the initial qualitative description of Harkins (1947), which was fleshed out in more quantitative terms by Smith and Ewart (1948). Although theory of emulsion polymerization has become much more intricate in the years since, the theory of Harkins, Smith and Ewart remains the best point of introduction and of departure. With recent advances in both emulsion kinetics and polymer characterization, more in-depth studies have been carried out on important aspects in emulsion polymerization and better understanding has been achieved. A good review on recent advances in emulsion kinetics was given by Gilbert (1995). Researchers have also expanded their work from homopolymerization to copolymerization and even terpolymerization. There is a large body of models in the literature that describes certain aspects of emulsion homo-/copolymerization (Gloor, 1996; Sayer, 1997, 2001; Yabuki, 2000; Gao, 2002; Zeaiter, 2002; Casella, 2003; Ginsburger, 2003; Alhamad, 2005).

It is generally accepted that any one of the mechanisms could be responsible for particle formation depending on the nature of the monomer and the amount of emulsifier used in the recipe. The processes that can be modeled using the Polymers Plus emulsion polymerization model are those that follow two common mechanisms for particle formation: micellar or homogeneous polymerization. Homogeneous polymerization should become progressively more important with increasing monomer solubility in water and decreasing amount of surfactants.

Usually, anionic emulsifiers and water-soluble persulfate initiators are used for particle nucleation by the micellar mechanism. Micellar nucleation is considered to be the primary mechanism for particle formation (Harkin, 1945; Smith & Ewart, 1948) in those emulsion polymerization systems for which the monomer is very sparingly soluble in water, and where the concentration of emulsifier is above the critical micelle concentration (CMC).

The monomers are dispersed in the form of droplets in the water by agitation. The droplets formed are stabilized by the emulsifier molecules which are absorbed on the droplet surface. In addition to the droplets, monomer is also found dissolved in the aqueous medium and solubilized inside the micelles. Similarly, the emulsifier is found in three locations: in the micelles, dissolved in the aqueous medium, and adsorbed on the monomer droplets. Since water soluble initiator is used, the initiator molecules will be mainly found dissolved in the water medium (Gilbert, 1995; Lovell, El-Aaser, 1997).

When a typical emulsion polymerization recipe is heated, the initiator dissociates in the aqueous medium and produces initiator radicals. Upon propagating with monomer in the water phase, the initiator radicals form oligomeric radicals and enter the micelles, which are aggregates of emulsifier molecules inside which a small amount of monomer is entrapped. The capturing of a radical by micelle and reaction with the entrapped monomer signifies the formation of a particle from a micelle (*stage I: Nucleation*) (Gilbert, 1995; Lovell, El-Aaser, 1997). The time required for particle nucleation to be complete is also called the nucleation time or the nucleation period, and usually lasts 10-15 minutes in conventional polymerization systems (Lovell, El-Aaser, 1997).

As the propagation takes place in the preformed seed particles, a thermodynamic potential difference is created for the diffusion of the monomer from the monomer droplets into the growing particles. The propagation stage (*stage II: Growth*) is also known as the growth stage of the reaction, and is responsible for the development of the properties of the emulsion polymer: molecular weight, composition, micro structure, etc. As the particles grow, some of the micelles disintegrate, and cover to stabilize them. Therefore, the micelles are not only consumed in the formation of polymer particles, but also in the stabilization of growing polymeric particles. As the particles grow, the

emulsifier molecules are continuously adsorbed into or desorbed from the particles to maintain thermodynamic equilibrium. Since the growth reaction lasts about 10-12 hours, there is great potential for optimizing the reaction time by increasing temperature or by keeping the particles saturated with monomer. The propagation stage is considered complete when the monomer droplets are totally depleted (Gilbert, 1995; Lovell, El-Aaser, 1997).

Since the number of particles remains constant and the particles are saturated with monomer, this stage is marked by a constant rate of polymerization and could easily be observed on a conversion versus time plot. Operational conditions can be chosen in such way that there are no monomer droplets in the reaction mixture. The condition is initially in the last stage of emulsion polymerization, where no monomer droplets are present. Only latex particles and the aqueous phase are present during this period, with the majority of the remaining monomer being confined to the latex particles, although a small amount (depending on the aqueous-phase solubility of the monomer) will be dissolved in the continuous phase. In the specific case of styrene-butadiene, which is sparsely water-soluble (water solubility of styrene and butadiene are 0.07 and 0.8 g/L), almost all monomer in the particle phase. The water solubility defines the amount of monomer available in the water phase to propagate the oligomeric polymerization. Particles as well as micelles are equally effective in capturing radicals from the aqueous phase. A growing radical can escape from a particle and return to the aqueous medium to participate in an aqueous phase termination reaction or enter into another particle. Radical generated in the aqueous phase are absorbed by the micelles during micellar nucleation and by the particle during nucleation and subsequent growth (Gilbert, 1995; Lovell, El-Aaser, 1997).

In the last stage (*stage III: Monomer Finishing*), the monomer finishing stage, the reaction mixture consists of the monomer swollen polymer particles and the aqueous medium. Further polymerization of the monomer in the particles takes place. During last stage, the concentration of monomer dissolved in the aqueous phase falls rapidly, as does the concentration in the polymer particles (Gilbert, 1995; Lovell, El-Aaser, 1997).

The polymerization of different monomers together to form a copolymer offers one of the simplest methods of improving (or at least changing) polymer properties, and one that has almost limitless variants. Obviously, the introduction of a second monomer brings with it the need to take into account the effects differences in monomer reactivity on the composition of the copolymer formed and the variation of copolymer composition with conversion. For emulsion polymerizations, the situation is more complex than bulk or solution polymerizations due to the heterogeneous nature of the reaction (Van Krevelen, 1990).

Many of the monomers are actually more useful when copolymerized. For example, the homopolymer of styrene is poor in its resistance to organic solvents and ability to undergo environmental degradation; these disadvantages, coupled with brittleness and low upper use temperatures, effectively disqualify it for a number of applications. Copolymerization is often an attempt to obtain properties intermediate between those of homopolymers. Simultaneous polymerization of two or more monomers is a powerful and commercially important process for creating polymers with tailor made properties.

3. Methodology

The simulation was based on a detailed fundamental model as developed by Broadhead, (1985) of a semi-batch reactor carrying out the free radical emulsion copolymerization of styrene and butadiene. This resulting latex system will be furthermore used for paper coating application. Nevertheless, this final application is not the main topic of this work. In this process, the seeded emulsion copolymerization of styrene and butadiene is carried out in a semi-batch reactor using ammonium persulfate (APS) as the water-soluble thermal initiator, sodium lauryl sulfate (SLS) as the anionic emulsifier, and tertiary dodecyl mercaptane (TDM) as a chain transfer agent. A schematic representation of the reactor is shown in Figure 1. It consists of a batch reactor with an initial batch charge at 20C, 10 bar (300 kg styrene, 300 kg butadiene, 30 kg SLS, 7 kg APS, 30 kg TDM, 1000 kg water) and a continuous feed at 20C, 10 bar (700 kg styrene, 700 kg butadiene, 100 kg SLS, 3 kg APS, 1000 kg water).

The regular operating procedure for such a reactor starts with changing an initial recipe of differential material. Then, the reaction mixture is heated up to its reaction temperature profile. Once

the reaction temperature is reached, monomers, initiator, emulsifier, and water start being fed according to some feed policies until the end of the batch. The batch duration is assumed to be 10 hours for all case studies in this work. The Polymer Non-Random Two Liquid activity coefficient model (POLYNRTL) is used as the physical property method. The thermo physical properties of the monomers are obtained from the Aspen Plus pure component databank. The polymer physical properties are calculated using the van Krevelen's method (van Krevelen, 1990). The reaction type and reaction schemes as outlined in Table 1; rate constant for the kinetic scheme are obtained from Broadhead (1985).

Figure 1. Reactor for Semi-batch Emulsion Copolymerization of Styrene-butadiene Rubber. (The CHARGE is a discontinuous stream)

Table 1. The Reaction Type and Reaction Scheme

Reaction type	Reaction scheme
Initiator decomposition	$I \rightarrow n.R^*$ Initiator $\rightarrow$ Radicals
Propagation	$P_n + M \rightarrow P_{n+1}$ Active segment + Adding monomer $\rightarrow$ New active segment
Chain transfer - monomer	$P_n + M \rightarrow D_n + PI$ Active segment + Transfer monomer $\rightarrow$ Dead chain + Active segment
Termination by combination	$P_n + P_m \rightarrow D_{n+m}$ Active segment + Active segment $\rightarrow$ Dead chain
Chain transfer agent	$P_n + A \rightarrow D_n + R^*$ Active segment + Transfer agent $\rightarrow$ Dead chain + Radical

The emulsion polymerization process is extremely complex and involves phenomena for which a complete theoretical understanding has not been reached. The important model features and assumptions used in the emulsion polymerization model in Polymers Plus shown in Table 2.

Table 2. Model Features and Assumptions in The Emulsion Polymerization Model in Polymers Plus

No.	Asumptions
1.	The reaction system is heterogeneous and formed by three phases: a monomer phase, an aqueous phase, and a polymer phase
2.	The reaction mixture is perfectly mixed.
3.	Particles are formed by the micellar mechanisms. Due to the high surfactant concentration and sparsely water-soluble monomers used in this work, the second type of nucleation (i.e. homogenous nucleation) is considered negligible
4.	No agglomeration or breakage of particles occurs
5.	No secondary nucleation occurs
6.	The polymerization follows the classical case 2 of the Smith-Ewart theory, which means that radical desorption is negligible and the average number of radicals per particle is equal to 0.5
7.	All particles have the same average number of radicals and hence the same volumetric growth rate
8.	The particle size distribution is unimodal (monodisperse population of polymer particles).
9.	The concentration of the monomers in different phases is at the thermodynamic equilibrium
10.	There are no mass transfer limitations on the polymerization reactions
11.	Molecular weight is controlled by chain transfer reactions
12.	Pseudo-steady state hypothesis is used for the radical balance in the aqueous phase
13.	Terminal copolymerization model is used

4. Results and Discussion

After 1 hour seeding step as an initial charge, simulation were carried out with 1 hour feeding time immediately after the end of seeding step with reaction temperature profile at 65°C from 0 to 0.5 hour, 70°C from 0.5 to 1 hour and 75°C from 1 to 10 hours (see Figures 2 and 3).

Figure 2. Total Mass and Continuous Feed Profile

Figure 3. Reaction Temperature Profile

The mass of monomers, polymer, and other ingredients in the reactor is shown in Figure 4.

Figure 4. The Mass Monomer, Polymer, and other Ingredients in the Reactor

Although the flow rates of styrene and butadiene are equal, the figure shows that butadiene reacts faster than styrene due to its higher reactivity. The mass flow of styrene and butadiene were calculated with the following equations:

$$-\lambda_1(1) = k_{11} \cdot [-M_1 \bullet] [M_1] + k_{21} \cdot [-M_2 \bullet] [M_1] \quad (1)$$

$$-\lambda_1(2) = k_{12} \cdot [-M_1 \bullet] [M_2] + k_{22} \cdot [-M_2 \bullet] [M_2] \quad (2)$$

Once nucleated (by whatever means), polymer particles adsorb more monomers to be able to maintain monomer volume fractions, approximated by the equilibrium swelling of the monomers in the polymer. Polymer particles thus grow over time and this requires more surfactant for stabilization, as does further nucleation of new particles. Micelles are in this manner progressively depleted. When they have vanished completely, the system comprises only polymer particles and monomer droplets. The disappearance of micelles signals the end of what are called stage I and the beginning of stage II. In stage I, micelles, polymer particles, and monomer droplets coexist, the number of polymer particles and their size increase at the expense of the micelles from 0 to 0.021 hour (see Figure 5a). The final number of particles is determined in this stage. The particle number is given by the following equation:

$$\frac{dv_0}{dt} = k_{am} A_m N_a [R \bullet]_w \quad (3)$$

In stage II and III, the concentration of polymer particles, stays constant while the polymerization proceeds (see Figure 5b). Polymerization occurs within the polymer particles, which maintain a nearly constant volume fraction of monomer. The incoming monomer is of course supplied by the monomer droplets via the aqueous solution. There will come a point, short of complete conversion, at which the total volume of monomer droplets are depleted after 2 hours reaction and it gradually goes to zero around 47% conversion, which marks the end of stage II. The only remaining monomer not in the polymer particles is in the aqueous phase. This marks the transition to stage III (see Figure 5c). As shown, the monomer droplets are completely depleted after 4 hours. The volume of the monomer droplet phase was calculated using the following equation.

$$V_m = \frac{(f_1 N_{m,1} + f_2 N_{m,2}) M_w}{d_{avg}} \quad (4)$$

where

$$d_{avg} = f_1 d_{m,1} + f_2 d_{m,2} \quad (5)$$

$$\frac{dN_{m,1}}{dt} = F_{m,1,in} - R_{p,1} V_p \quad (6)$$

$$\frac{dN_{m,2}}{dt} = F_{m,2,in} - R_{p,2}V_p \quad (7)$$

$$R_{p,1} = \frac{k_{p,11}k_{p,22}(r_1C_{p,1}^2 + C_{p,1}C_{p,2})\bar{n}N_{tot}}{k_{p,22}r_1C_{p,1} + k_{p,11}r_2C_{p,2}} \frac{N_aV_p}{N_aV_p} \quad (8)$$

$$R_{p,2} = \frac{k_{p,11}k_{p,22}(r_2C_{p,2}^2 + C_{p,1}C_{p,2})\bar{n}N_{tot}}{k_{p,22}r_1C_{p,1} + k_{p,11}r_2C_{p,2}} \frac{N_aV_p}{N_aV_p} \quad (9)$$

As expected, the volume of the swollen polymer phase decreases slightly after the depletion of the monomer droplets. This last stage comprises the consumption of the remaining monomer. The total volume of polymer particles increases before 47% conversion due to particle growth in stages I and II. It then decreases after 47% (in stage III) due to the density difference between monomer and polymer. The total volume of the aqueous phase remains nearly constant throughout the entire reaction and was calculated with the following equation:

$$V_w = \frac{V_{w0}}{1 - (M_{w,1}/C_{w,1}) - (M_{w,2}/C_{w,2})} \quad (10)$$

This division of an ideal emulsion polymerization into three intervals is helpful generalization implicit in the early theories.

(a)

(b)

Figure 5. Three Stages of Emulsion Polymerization, Represented in terms of (a) the Number of Particles Focusing on The Nucleation Stage, (b) The Number of Particles focusing on The Total Reaction Time and (c) Total Volume of The Monomer, Polymer and Aqueous Phase in The Reactor

As previously mentioned, the starting point is *case 2* kinetics and assumes that radical desorption is negligible. In the immediate termination of two radicals that occurs in this case, the two radicals are not equivalent; rather, one was a resident in the particle for some time and the other is a new arrival. The resident chains will be relatively long (and will have a geometric distribution), whereas the newly arrived chains will be short. The resulting dead chain distribution will depend on the termination mechanism, as usual. If combination is dominant, each of the resident chain upon dying is increased by some small number of units, and the geometric distribution is roughly preserved, which will have a polydispersity (PDI) of approximately 2 (see Figure 6a). The final product has the average degree of polymerization of 1485.39 for number average degree of polymerization (DP_n) and 3353.34 for weight average degree of polymerization DP_w (see Figure 6b). The polydispersity, number average and weight average degree of polymerization were calculated using the following equations:

$$PDI = \frac{DP_w}{DP_n} \quad (11)$$

$$DP_n = \frac{\lambda_1}{\lambda_0} \quad (12)$$

$$DP_w = \frac{\lambda_2}{\lambda_1} \quad (13)$$

Figure 6. (a) The Polydispersity, (b) The Number Average and Weight Average Degree of Polymerization

At the end of the reaction, the final polymer product has 43% solid content with overall conversion of 89% (see Figure 7), the average molecular weight of 104024.36 for number average of molecular weight (M_n), 234840.28 for weight average of molecular weight (M_w) and 70.16 for the segment (see Figure 8).

Figure 7. The Solid Content (Liquid Polymer) versus Time

The number-and-weight average molecular weight of the copolymer as well as copolymer average segment molecular weight were calculated using the following equations.

$$M_n = DP_n \bar{M}_{seg} \quad (14)$$

$$M_w = DP_w \bar{M}_{seg} \quad (15)$$

$$\bar{M}_{seg} = \sum_i F_p(i) M_i \quad (16)$$

Figure 8. (a) The Average Molecular Weight and (b) The Average Segment Molecular Weight versus Time

5. Conclusions

The simulation provides the base case of a styrene-butadiene seeded emulsion copolymerization process in a semi-batch reactor, which can be used to study various process variables, and operating conditions affect the product quality during the course of a semi-batch reactor in the research and development, engineering or production. The extensiveness of the database of this simulation package is the most important feature that makes this model distinct from most other models presented in the literature.

The limit of the simulation progress depends on one understanding of the process. One could use it to optimize and control the final product quality through selection of process variable and operating condition trajectories.

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Notations

CHARGE	= initial charge stream
CFEED	= continuous feed stream
PROD	= production stream
A_m	= area of micelles (m^2/m^3 of aqueous phase)
d_{avg}	= average density of the monomers
$\bar{n}$	= average number of radicals per particle
N_a	= avogadro number
$d_i^{m,i}$	= density of monomer i
f_1	= mole fraction of monomer 1 in the comonomer mixture
f_2	= mole fraction of monomer 2 in the comonomer mixture
M_w	= monomer concentration in aqueous phase
$N_{m,1}$	= number of moles monomer 1
$N_{m,2}$	= number of moles monomer 2
$[R\bullet]_v$	= radical concentration in the aqueous phase
k_p	= rate constant for propagation in particle phase
k_{am}	= rate constant for the absorption of radicals by micelles
$R_{p,1}$	= rates of reaction for monomer 1 in the particle
$R_{p,2}$	= rates of reaction for monomer 2 in the particle
V_m	= volume of the monomer phase
V^p	= volume of the polymer phase
V_{wo}	= volume of the water phase
$\bar{M}_{seg}$	= average segment molecular weight
λ_2	= first moment of chain length distribution
$\lambda_1(i)$	= mass flow of segments of monomer i
$F_p(i)$	= mole segment fraction of segments of type i in the copolymer
M_i	= molecular weight of segment type in the copolymer
k_{12}, k_{21}	= rate coefficients for the cross-propagation reactions
k_{11}, k_{22}	= rate coefficients for the homopropagation reactions

λ_3	= second moment of chain length distribution
$[-M, \bullet]$	= the total concentrations of propagating chains with terminal i -type active centre
λ_1	= zeroth moment of chain length distribution
v_0	= zeroth moment of the particle size distribution

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